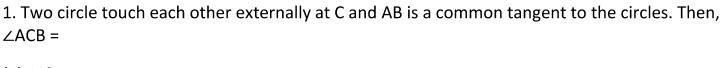


Important Questions

Multiple Choice questions-



- (a) 60°
- (b) 45°
- (c) 30°
- (d) 90°
- 2. If TP and TQ are two tangents to a circle with centre O so that \angle POQ = 110°, then, \angle PTQ is equal to
- (a) 60°
- (b) 70°
- (c) 80°
- (d) 90°
- 3. Tangents from an external point to a circle are
- (a) equal
- (b) not equal
- (c) parallel
- (d) perpendicular
- 4. Two parallel lines touch the circle at points A and B respectively. If area of the circle is 25 n cm², then AB is equal to

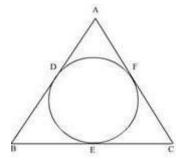
Swotters

- (a) 5 cm
- (b) 8 cm
- (c) 10 cm
- (d) 25 cm

5. A line through point of contact and passing through centre of circle is known as
(a) tangent
(b) chord
(c) normal
(d) segment
6. A tangent PQ at a point P of a circle of radius 5 cm meets a line through the centre O at a point Q
(a) √119 cm
(b) 13 cm
(c) 12 cm
(d) 8.5 cm
7. From a point P which is at a distance of 13 cm from the centre O of a circle of radius 5 cm, the pair of tangents PQ and PR to the circle are drawn. Then the area of the quadrilateral PQOR is
(a) 60 cm ²
(b) 65 cm ²
(c) 30 cm ²
(d) 32.5 cm ²
8. At point A on a diameter AB of a circle of radius 10 cm, tangent XAY is drawn to the circle. The length of the chord CD parallel to XY at a distance 16 cm from A is
(a) 8 cm
(b) 10 cm
(c) 16 cm
(d) 18 cm
9. The tangents drawn at the extremities of the diameter of a circle are
(a) perpendicular

- (b) parallel
- (c) equal
- (d) none of these

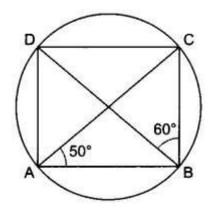
10. A circle is inscribed in a \triangle ABC having AB = 10cm, BC = 12cm and CA = 8cm and touching these sides at D, E, F respectively. The lengths of AD, BE and CF will be



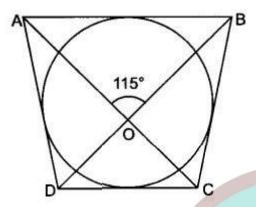
- (a) AD = 4cm, BE = 6cm, CF = 8cm
- (b) AD = 5cm, BE = 9cm, CF = 4cm
- (c) AD = 3cm, BE = 7cm, CF = 5cm
- (d) AD = 2cm, BE = 6cm, CF = 7cm

Very Short Questions:

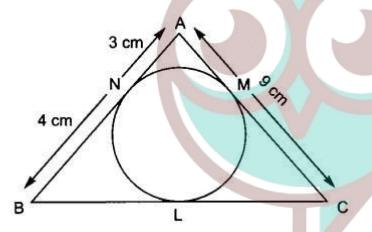
- 1. If a point P is 17 cm from the centre of a circle of radius 8 cm, then find the length of the tangent drawn to the circle from point P.
- 2. The length of the tangent to a circle from a point P, which is 25 cm away from the centre, is 24 cm. What is the radius of the circle?
- 3. In Fig, ABCD is a cyclic quadrilateral. If $\angle BAC = 50^{\circ}$ and $\angle DBC = 60^{\circ}$ then find $\angle BCD$.



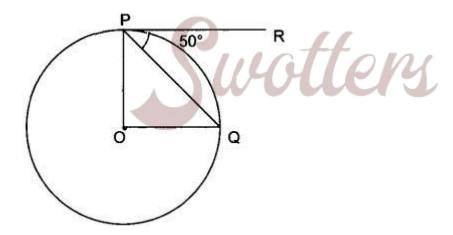
4. In Fig. the quadrilateral ABCD circumscribes a circle with centre O. If \angle AOB = 115°, then find \angle COD.



5. In Fig. AABC is circumscribing a circle. Find the length of BC.

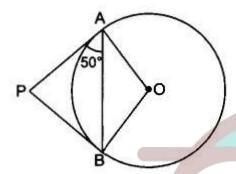


6. In Fig. O is the centre of a circle, PQ is a chord and the tangent PR at P makes an angle of 50° with PQ. Find ∠POQ.



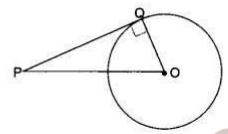
- 7. If two tangents inclined at an angle 60° are drawn to a circle of radius 3 cm, then find the length of each tangent.
- **8.** If radii of two concentric circles are 4 cm and 5 cm, then find the length of each chord of one circle which is tangent to the other circle.

- **9.** PQ is a tangent drawn from a point P to a circle with centre O and QOR is a diameter of the circle such that \angle POR = 120° then find \angle OPQ.
- **10.** From an external point P, tangents PA and PB are drawn to a circle with centre O. If $\angle PAB = 50^{\circ}$, then find $\angle AOB$.

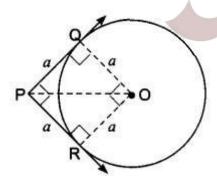


Short Questions:

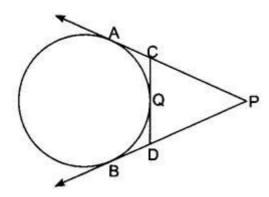
- 1. AB is a diameter of a circle and AC is its chord such that ∠BAC = 30°. If the tangent at C intersects AB extended at D, then BC = BD.
- 2. The length of tangent from an external point P on a circle with centre O is always less than OP.



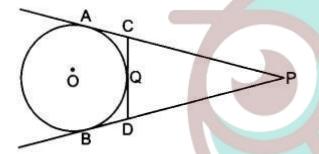
3. If angle between two tangents drawn from a point P to a circle of radius 'a' and centre 0 is 90° , then OP = aV2.



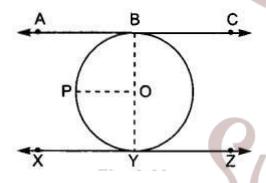
4. In Fig. PA and PB are tangents to the circle drawn from an external point P. CD is the third tangent touching the circle at Q. If PA = 15 cm, find the perimeter of Δ PCD.



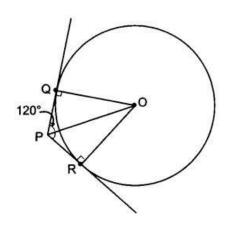
5. In Fig. PA and PB are tangents to the circle from an external point P. CD is another tangent touching the circle at Q. If PA = 12 cm, QC = QD = 3 cm, then find PC + PD.



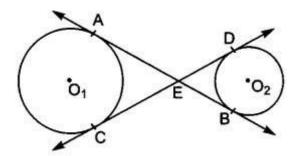
6. Prove that the line segment joining the points of contact of two parallel tangents of a circle, passes through its centre.



7. If from an external point P of a circle with centre 0, two tangents PQ and PR are drawn such that QPR = 120°, prove that 2PQ = PO.



8. In Fig. common tangents AB and CD to two circles with centres , and 0, intersect at E. Prove that AB = CD.

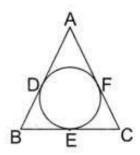


9. The incircle of an isosceles triangle ABC, in which AB = AC, touches the sides BC, CA and AB at D, E and F respectively. Prove that BD = DC.

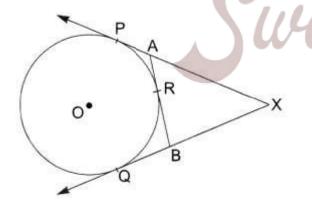
OR

In Fig. if AB = AC, prove that BE = EC.

[Note: D, E, F replace by F, D, E]



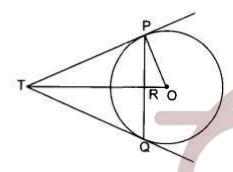
10. In Fig. XP and XQ are two tangents to the circle with centre O, drawn from an external point X. ARB is another tangent, touching the circle at R. Prove that XA + AR = XB + BR.



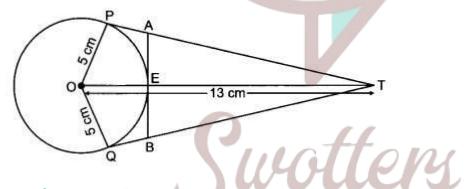
Long Questions:

1. Prove that the tangent to a circle is perpendicular to the radius through the point of contact.

- 2. Prove that the lengths of two tangents drawn from an external point to a circle are equal.
- **3.** Prove that the parallelogram circumscribing a circle is a rhombus.
- **4.** In Fig. PQ is a chord of length 16 cm, of a circle of radius 10 cm. The tangents at P and Q intersect at a point T. Find the length of TP.

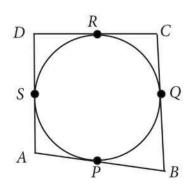


- 5. If PQ is a tangent drawn from an external point P to a circle with centre O and QOR is a diameter where length of QOR is 8 cm such that \angle POR = 120°, then find OP and PQ.
- 6. In Fig. O is the centre of a circle of radius 5 cm. T is a point such that OT = 13 cm and OT intersects circle at E. If AB is a tangent to the circle at E, find the length of AB, where TP and TQ are two tangents to the circle.



Case Study Questions:

1. In a park, four poles are standing at positions A, B, C and D around the fountain such that the cloth joining the poles AB, BC, CD and DA touches the fountain at P, Q, R and S respectively as shown in the figure.





Based on the above information, answer the following questions.

- i. If O is the centre of the circular fountain, then ∠OSA
 - a. 60º
 - b. 90º
 - c. 45º
 - d. None of these
 - ii. Which of the following is correct?

a.
$$AS = AP$$

b.
$$P = BQ$$

c.
$$CQ = CR$$

- d. All of these
- iii. If DR = 7cm and AD= 11cm, then AP =
 - a. 4cm
 - b. 18cm
 - c. 7cm
 - d. 11cm



- iv. If O is the centre of the fountain, with $\angle QCS=60^{\circ}$, then $\angle QOS$
 - a. 60º
 - b. 120º
 - c. 90º
 - d. 30º
- v. Which of the following is correct?

a.
$$AB + BC = CD + DA$$

b.
$$AB + AD = BC + CD$$

- c. AB + CD = AD + BC
- d. All of these
- 2. Smita always finds it confusing with the concepts of tangent and secant of a circle. But this time she has determined herself to get concepts easier. So, she started listing down the differences betwee tangent and secant of a circle, along with their relation. Here, some points in question form are list by Smita in her notes. Try answering them to clear your concepts also.



- i. A line that intersects a circle exactly at two points is called:
 - a. Secant
 - b. Tangent
 - c. Chord
 - d. Both (a) and (b)
- ii. Number of tangents that can be drawn on a circle is:
 - a. 1
 - b. 0

- c. 2
- d. Infinite
- iii. Number of tangents that can be drawn to a circle from a point not on it, is:
 - a. 1
 - b. 2
 - c. 0
 - d. Infinite
- iv. Number of secants that can be drawn to a circle from a point on it is:
 - a. Infinite
 - b. 1
 - c. 2
 - d. 0
- v. A line that touches a circle at only one point is called:
 - a. Secant
 - b. Chord
 - c. Tangent
 - d. Diameter

Assertion Reason Questions-

of reason (R). Mark the correct choice as:

1. Directions: In the following questions, a statement of assertion (A) is followed by a statement

- a. Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
- b. Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
- c. Assertion (A) is true but reason (R) is false.
- d. Assertion (A) is false but reason (R) is true.

Assertion (A): In a circle of radius 6 cm, the angle of a sector is 60° . Then the area of the sector is $132/7 \text{ cm}^2$.

Reason (R): Area of the circle with radius r is πr^2

2. Directions: In the following questions, a statement of assertion (A) is followed by a statement

of reason (R). Mark the correct choice as:

- a. Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
- b. Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
- c. Assertion (A) is true but reason (R) is false.
- d. Assertion (A) is false but reason (R) is true.

Assertion (A): If the circumference of a circle is 176 cm, then its radius is 28 cm.

Reason (R): Circumference $2\pi \times$ radius.



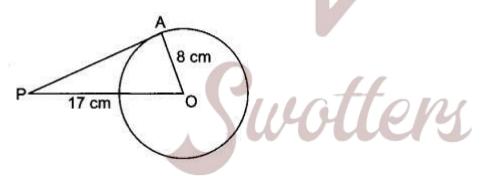
Answer Key-

Multiple Choice questions-

- **1.** (d) 90°
- **2.** (b) 70°
- **3.** (a) equal
- **4.** (c) 10 cm
- **5.** (c) normal
- **6.** (a) √119 cm
- 7. (a) 60 cm^2
- **8.** (c) 16 cm
- 9. (b) parallel
- **10.** (a) AD = 4cm, BE = 6cm, CF = 8cm

Very Short Answer:

1.



 $OA \perp PA$ (: radius is \perp to tangent at point of contact)

 \therefore In \triangle OAP, we have

$$PO^2 = PA^2 + AO^2$$

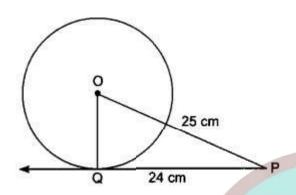
$$\Rightarrow$$
 (17)² = (PA)² + (8)²

$$(PA)^2 = 289 - 64 = 225$$

$$\Rightarrow$$
 PA = $\sqrt{225}$ = 15

Hence, the length of the tangent from point P is 15 cm.

2.



$$: OQ \perp PQ$$

$$\therefore$$
 PQ2 + QO2 = OP2

$$\Rightarrow$$
 252 = OQ2 + 242

or
$$OQ = \sqrt{625} - \sqrt{576}$$

$$= \sqrt{49} = 7 \text{ cm}$$

Here $\angle BDC = \angle BAC = 50^{\circ}$ (angles in same segment are equal) 3.

In ABCD, we have

$$\angle$$
BCD = 180° - (\angle BDC + \angle DBC)

$$= 180^{\circ} - (50^{\circ} + 60^{\circ}) = 70^{\circ}$$

∴ ∠AOB = ∠COD (vertically opposite angles) 4.

5. AN = AM = 3 cm [Tangents drawn from an external point]

BN = BL = 4 cm [Tangents drawn from an external point]

$$CL = CM = AC - AM = 9 - 3 = 6 cm$$

$$\Rightarrow$$
 BC = BL + CL = 4 + 6 = 10 cm.

6.
$$\angle OPQ = 90^{\circ} - 50^{\circ} = 40^{\circ}$$

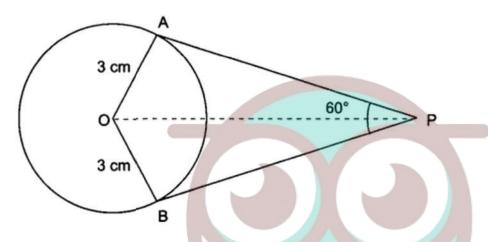
$$\angle OPQ = \angle OQP = 40^{\circ}$$

(Equal opposite sides have equal opposite angles)

$$\angle POQ = 180^{\circ} - \angle OPQ - \angle OQP$$

$$= 180^{\circ} - 40^{\circ} - 40^{\circ} = 100^{\circ}$$

7.



 $\triangle AOP \cong \triangle BOP$ (By SSS congruence criterion)

$$\angle APO = \angle BPO = \frac{60^{\circ}}{2} = 30^{\circ}$$

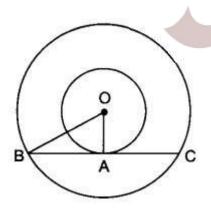
In $\triangle AOP$, $OA \perp AP$

∴ tan 30° =
$$\frac{OA}{AP}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{3}{AP}$$

$$\Rightarrow$$
 AP = 3 $\sqrt{3}$ cm

8.



$$OA = 4 \text{ cm}, OB = 5 \text{ cm}$$

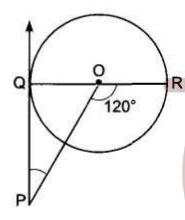
$$\therefore$$
 OB2 = OA2 + AB2

$$\Rightarrow$$
 52 = 42 + AB2

$$\Rightarrow$$
 AB = $\sqrt{25} - \sqrt{16} = 3$ cm

$$\Rightarrow$$
 BC = 2 AB = 2 \times 3 = 6 cm

9.



$$\angle OQP = 90^{\circ}$$

$$\angle QOP = 180^{\circ} - 120^{\circ} = 60^{\circ}$$

$$\angle OPQ = 180^{\circ} - \angle OQP - \angle QOP$$

$$= 180^{\circ} - 90^{\circ} - 60^{\circ}$$

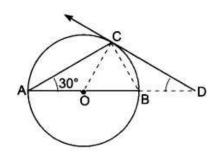
10. :
$$PA = PB \Rightarrow \angle BAP = \angle ABP = 50^{\circ}$$

$$\therefore \angle APB = 180^{\circ} - 50^{\circ} - 50^{\circ} = 80^{\circ}$$

$$\therefore \angle AOB = 180^{\circ} - 80^{\circ} = 100^{\circ}$$

Short Answer:

1.



True, Join OC,

∠ACB = 90° (Angle in semi-circle)

$$\therefore \angle OBC = 1800 - (90^{\circ} + 30^{\circ}) = 60^{\circ}$$

Since, OB = OC = radii of same circle [Fig. 8.16]

$$\therefore \angle OBC = \angle OCB = 60^{\circ}$$

$$\Rightarrow \angle BCD = 90^{\circ} - 60^{\circ} = 30^{\circ}$$

Now, $\angle OBC = \angle BCD + \angle BDC$ (Exterior angle property)

$$\Rightarrow$$
 60° = 30° + \angle BDC

$$\Rightarrow$$
 \angle BDC = 30°

$$\therefore$$
 \angle BCD = \angle BDC = 30°

$$\therefore$$
 BC = BD

2. True, let PQ be the tangent from the external point P.

Then $\triangle PQO$ is always a right angled triangle with OP as the hypotenuse. So, PQ is always less than OP.

3. True, let PQ and PR be the tangents

Since
$$\angle P = 90^{\circ}$$
, so $\angle QOR = 90^{\circ}$

Also,
$$OR = OQ = a$$

∴ PQOR is a square

$$\Rightarrow OP = \sqrt{a^2 + a^2} = \sqrt{2a^2} = a\sqrt{2}$$

4. : PA and PB are tangent from same external point

Now, Perimeter of $\triangle PCD = PC + CD + DP = PC + CQ + QD + DP$

$$= PC + CA + DB + DP$$

$$= PA + PB = 15 + 15 = 30 cm$$

5. PA = PC + CA = PC + CQ [: CA = CQ (tangents drawn An from external point are equal)]

$$\Rightarrow$$
 12 = PC + 3 = PC = 9 cm

$$\therefore$$
 PA = PB = PA - AC = PB - BD

$$\Rightarrow$$
 PC = PD

Hence, PC + PD = 18 cm

6. Let the tangents to a circle with centre O be ABC and XYZ.

Construction: Join OB and OY.

Draw OP||AC

Since AB | | PO

 \angle ABO + \angle POB = 180° (Adjacent interior angles)

∠ABO = 90° (A tangent to a circle is perpendicular to the radius through the point of contact)

$$90^{\circ} + \angle POB = 180^{\circ} = \angle POB = 90^{\circ}$$

Similarly ∠POY = 90°

$$\angle POB + \angle POY = 90^{\circ} + 90^{\circ} = 180^{\circ}$$

Hence, BOY is a straight line passing through the centre of the circle.

7. Given, ∠QPR = 120°

Radius is perpendicular to the tangent at the point of contact.

$$\angle$$
OQP = 90°

(Tangents drawn to a circle from an external point are equally inclined to the segment, joining the centre to that point)

In
$$\triangle QPO$$
, $\cos 60^\circ = \frac{PQ}{PO} \implies \frac{1}{2} = \frac{PQ}{PO}$

$$2PQ = PO$$

8. AE = CE and BE = ED [Tangents drawn from an external point are equal]

On addition, we get

$$AE + BE = CE + ED$$

$$\Rightarrow$$
 AB = CD

9.



Given, AB = AC

We have,
$$BF + AF = AE + CE(i)$$

AB, BC and CA are tangents to the circle at F, D and E respectively.

From (i) and (ii)

$$BD + AE = AE + CD (: AF = AE)$$

$$\Rightarrow$$
 BD = CD

In the given figure, 10.

$$AP = AR$$

$$BR = BQ$$

XP = XQ [Tangent to a circle from an external point are equal]

$$XA + AP = XB + BQ$$

$$XA + AR = XB + BR [AP = AR, BQ = BR]$$

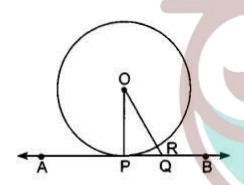
Long Answer:

1. Given: A circle C(O,r) and a tangent AB at a point P.

To Prove: OP \perp AB.

Construction: Take any point I, other than P, on the tangent AB. Join OQ. Suppose OQ meets the circle at R.

Proof: We know that among all line segments joining the point to a point on AB, the shortest one is perpendicular to AB. So, to prove that OP \perp AB it is sufficient to prove that OP is shorter than any other segment joining O to any point of AB.



Clearly, OP = OR [Radii of the same circle]

Now, OQ = OR + RQ

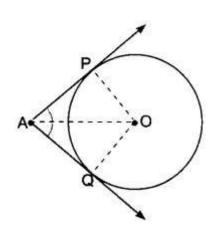
 \Rightarrow OQ > OR

 \Rightarrow OQ > OP [:OP = OR]

Thus, OP is shorter than any other segment joining O to any point on AB.

Hence, OP \perp AB.

2.



Given: AP and AQ are two tangents from a point A to a circle C (O, r).

To Prove: AP = AQ

Construction: Join OP, OQ and OA.

Proof: In order to prove that AP = AQ, we shall first prove that \triangle OPA \cong \triangle OQA.

Since a tangent at any point of a circle is perpendicular to the radius through the point of contact.

 \therefore OP \perp AP and OQ \perp AQ

$$\Rightarrow \angle OPA = \angle OQA = 90^{\circ}$$

Now, in right triangles OPA and OQA, we have

OP = OQ [Radii of a circle]

 $\angle OPA = \angle OQA [Each 90^{\circ}]$

and OA = OA [Common]

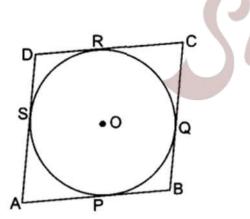
So, by RHS-criterion of congruence, we get

 $\Delta OPA \cong OQA$

$$\Rightarrow$$
 AP = AQ [CPCT]

Hence, lengths of two tangents from an external point are equal.

3.



Let ABCD be a parallelogram such that its sides touch a circle with centre O.

We know that the tangents to a circle from an exterior point are equal in length.

Therefore, we have

AP = AS [Tangents from A]

BP = BQ [Tangents from B] (ii)

CR = CQ [Tangents from C] (iii)

And DR = DS [Tangents from D] (iv)

Adding (i), (ii), (iii) and (iv), we have

$$(AP + BP) + (CR + DR) = (AS + DS) + (BQ + CQ)$$

$$AB + CD = AD + BC$$

AB + AB = BC + BC [: ABCD is a parallelogram : AB = CD, BC = DA]

$$2AB = 2BC \Rightarrow AB = BC$$

Thus, AB = BC = CD = AD

Hence, ABCD is a rhombus.

4.

To find: TP

$$PR = RQ = \frac{16}{2} = 8 \text{ cm}$$
 [Perpendicular from the centre bisects the chord]

In $\triangle OPR$

$$OR = \sqrt{OP^2 - PR^2}$$

$$= \sqrt{10^2 - 8^2} = \sqrt{100 - 64}$$

$$= \sqrt{36} = 6 \text{ cm}$$

Let $\angle POR$ be θ

In
$$\triangle POR$$
, $\tan \theta = \frac{PR}{RO} = \frac{8}{6}$
 $\tan \theta = \frac{4}{3}$

We know, $OP \perp TP$ (Point of contact of a tangent is perpendicular to the line from the centre)

In
$$\triangle OTP$$
, $\tan \theta = \frac{OP}{TP} \Rightarrow \frac{4}{3} = \frac{10}{TP}$

$$TP = \frac{10 \times 3}{4} = \frac{15}{2} = 7.5 \text{ cm}.$$

5. Let O be the centre and QOR = 8 cm is diameter of a circle. PQ is tangent such that $\angle POR = 120^{\circ}$

Now, $OQ = OR = \frac{8}{2} = 4 \text{ cm}$

$$\angle POQ = 180 - 120^{\circ} = 60^{\circ}$$
 (Linear pair)

Also

$$OQ \perp PQ$$

Now, in right ΔPOQ .

$$\cos 60^{\circ} = \frac{OQ}{PO}$$

$$\Rightarrow \frac{1}{2} = \frac{OQ}{PO} \Rightarrow \frac{1}{2} = \frac{4}{PO}$$

$$\Rightarrow$$

$$PO = 8 \text{ cm}.$$

Again,
$$\tan 60^\circ = \frac{PQ}{OQ} \implies \sqrt{3} = \frac{PQ}{4}$$

$$\Rightarrow PQ = 4\sqrt{3}$$
 cm.

6. In right $\triangle POT$

$$PT = \sqrt{OT^2 - OP^2}$$

$$PT = \sqrt{169 - 25} = 12 \text{ cm and}$$

$$TE = 8 cm$$

Let
$$PA = AE = x$$

(Tangents from an external point to a circle are equal)

In right ΔAET

$$TA^2 = TE^2 + EA^2$$

$$\Rightarrow (12 - x)^2 = 64 + x^2$$

$$\Rightarrow$$
 144 + x^2 - 24 x = 64 + x^2

$$\Rightarrow x = \frac{80}{24}$$

$$\Rightarrow$$
 x = 3.3 cm

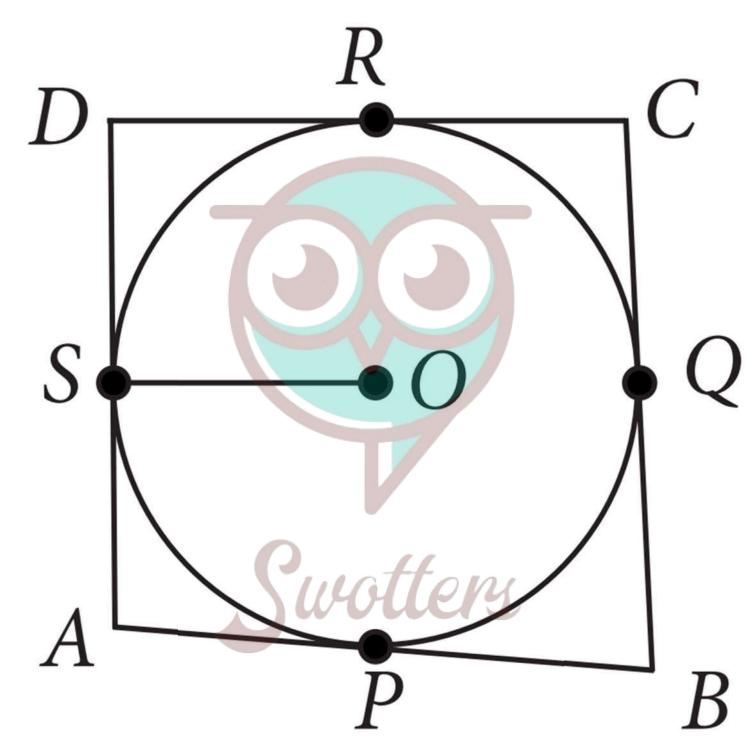
Thus, AB = 6.6 cm

Case Study Answer:

1. Answer:

i. (b) 90º

Solution:



Here, OS the is radius of circle.

Since radius at the point of contact is perpendicular to tangent So, \angle OSA=90°

ii. (d) All of these

Solution:

Since, length of tangents drawn from an external point to a circle are equal.

$$\therefore$$
 AS = AP, BP = BQ,

iii. (a) 4cm

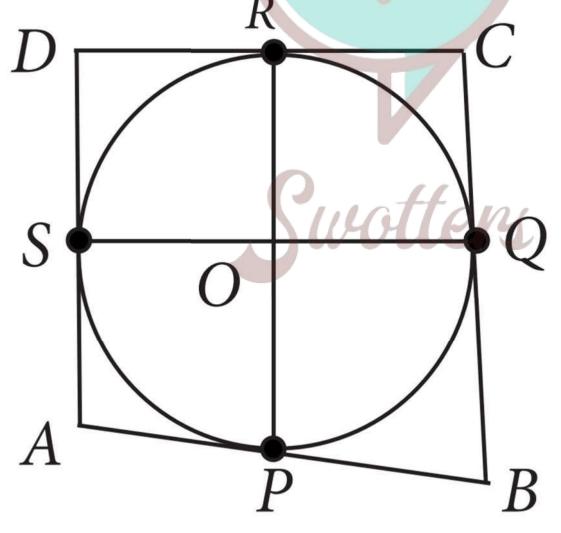
Solution:

$$AP = AS = AD - DS = AD - DR = 11 - 7 = 4cm$$
.

iv. (b) 120º

Solution:

In quadrilateral OQCR,



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$$\angle$$
QCR = 60°, (Given)

And
$$\angle OQC = \angle ORC = 90^{\circ}$$

[Since, radius at the point of contact is perpendicular to tangent.]

$$\therefore \angle QCR = 360^{\circ} - 90^{\circ} - 90^{\circ} - 60^{\circ} = 120^{\circ}$$

v. (c)
$$AB + CD = AD + BC$$

Solution:

From (I), we have AS = AP, DS = DR, BQ = BP and CQ = CR

Adding all above equations, we get

$$AS + DS + BQ + CQ = AP + DR + BP + CR$$

$$\Rightarrow$$
 AD + BC = AB + CD

2. Answer:

- i. (a) Secant
- ii. (d) Infinite
- iii. (b) 2
- iv. (a) Infinite
- (c) Tangent ٧.

Assertion Reason Answer-

- 1. (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
- 2. (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).