MATHEMATICS



Important Questions

Multiple Choice questions-

Question 1. Can we write 0 in the form of p/q?

- a. Yes
- b. No
- c. Cannot be explained
- d. None of the above

Question 2. The three rational numbers between 3 and 4 are:

- a. 5/2,6/2,7/2
- b. 13/4,14/4,15/4
- c. 12/7,13/7,14/7
- d.11/4,12/4,13/4

Question 3. In between any two numbers there are:

- a. Only one rational number
- b. Many rational numbers
- c. Infinite rational numbers
- d. No rational number

Question 4. Every rational number is:

- a. Whole number
- b. Natural number
- c. Integer
- d. Real number

Question 5. $\sqrt{9}$ is a number.

- a. Rational
- b. Irrational
- c. Neither rational or irrational
- d. None of the above

Question 6. Which of the following is an irrational number?

- a. $\sqrt{16}$
- b. $\sqrt{(12/3)}$

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- c. $\sqrt{12}$
- d. $\sqrt{100}$

Question 7. $3\sqrt{6} + 4\sqrt{6}$ is equal to:

- a. 6_V6
- b. 7_V6
- c. 4V12
- d. 7 $\sqrt{12}$

Question 8. $\sqrt{6}$ x $\sqrt{27}$ is equal to:

- a. 9√2
- b. 3√3
- c. 2√2
- d. 9_V3

Question 9. Which of the following is equal to x3?

- a. x^6-x^3
- b. x⁶.x³
- c. x^6/x^3
- d. $(x^6)^3$

Question 10. Which of the following are irrational numbers?

- a. $\sqrt{23}$
- b. $\sqrt{225}$
- c. 0.3796
- d. 7.478478

Very Short:

- 1. Simplify: $(\sqrt{5} + \sqrt{2})^2$.
- 2. Find the value of $\sqrt{(3)^{-2}}$.
- 3. Identify a rational number among the following numbers:
- 4. Express 1.8181... in the form $\frac{P}{q}$ where p and q are integers and q \neq 0.
- 5. Simplify: $\sqrt{45} 3\sqrt{20} + 4\sqrt{5}$
- 6. Find the value of'

$$\frac{(0.6)^0 - (0.1)^{-1}}{\left(\frac{3}{8}\right)^{-1} \left(\frac{3}{2}\right)^3 + \left(-\frac{1}{3}\right)^{-1}}$$

7. Find the value of.

$$\frac{4}{(216)^{\frac{-2}{3}}} - \frac{1}{(256)^{\frac{-3}{4}}}$$

Short Questions:

- Evaluate: $(\sqrt{5} + \sqrt{2^2} + (\sqrt{8} \sqrt{5})^2$
- Express 23.43 in $\frac{P}{q}$ Form, where p, q are integers and q \neq 0. 2.
- Let 'a' be a non-zero rational number and 'b' be an irrational number. Is 'ab' necessarily 3. an irrational? Justify your answer with example.
- Let x and y be a rational and irrational numbers. Is x + y necessarily an irrational 4. number? Give an example in support of your answer.
- 5. Represent $\sqrt{3}$ on the number line.
- 6. Represent $\sqrt{3.2}$ on the number line.
- Express 1.32 + 0.35 as a fraction in the simplest form. 7.

Long Questions:

If
$$x = \frac{\sqrt{p+q} + \sqrt{p-q}}{\sqrt{p+q} - \sqrt{p-q}}$$
, then prove that $q^2 - 2px + 9 = 0$.

If a =
$$\frac{1}{3-\sqrt{11}}$$
 and b = $\frac{1}{a}$, then find $a^2 - b^2$

3. Simplify

Simplify
$$\frac{3\sqrt{2}}{\sqrt{6}-\sqrt{3}} - \frac{4\sqrt{3}}{\sqrt{6}-\sqrt{2}} + \frac{2\sqrt{3}}{\sqrt{6}+2}$$

4. Prove that:

$$\frac{1}{1+\sqrt{2}} + \frac{1}{\sqrt{2}+\sqrt{3}} + \frac{1}{\sqrt{3}+\sqrt{4}} + \dots + \frac{1}{\sqrt{8}+3} = 2.$$

5. Find a and b, if

$$\frac{2\sqrt{5} + \sqrt{3}}{2\sqrt{5} - \sqrt{3}} + \frac{2\sqrt{5} - \sqrt{3}}{2\sqrt{5} + \sqrt{3}} = a + \sqrt{15}b$$

Assertion and Reason Questions-

MATHEMATICS NUMBER SYSTEM

- **1.** In these questions, a statement of assertion followed by a statement of reason is given. Choose the correct answer out of the following choices.
 - a) Assertion and reason both are correct statements and reason is correct explanation for assertion.
 - b) Assertion and reason both are correct statements but reason is not correct explanation for assertion.
 - c) Assertion is correct statement but reason is wrong statement.
 - d) Assertion is wrong statement but reason is correct statement.

Assertion: 0.271 is a terminating decimal and we can express this number as 271/1000 which is of the form p/q, where p and q are integers and $q \neq 0$.

Reason: A terminating or non-terminating decimal expansion can be expressed as rational number.

- **2.** In these questions, a statement of assertion followed by a statement of reason is given. Choose the correct answer out of the following choices.
 - a) Assertion and reason both are correct statements and reason is correct explanation for assertion.
 - b) Assertion and reason both are correct statements but reason is not correct explanation for assertion.
 - c) Assertion is correct statement but reason is wrong statement.
 - d) Assertion is wrong statement but reason is correct statement.

Assertion: Every integer is a rational number.

Reason: Every integer 'm' can be expressed in the form m/1.

Answer Key:

MCQ:

- 1. (a) Yes
- 2. (b) 13/4,14/4,15/4
- 3. (c) Infinite rational numbers
- 4. (d) Real number
- 5. (a) Rational
- 6. (c) √12
- 7. (b) 7v6
- 8. (a) 9√2

9. (c) x6/x3

10.(a) v23

Very Short Answer:

1. Here, $(\sqrt{5} + \sqrt{22} = (\sqrt{52} + 2\sqrt{5}\sqrt{2} + (\sqrt{2})2)$

$$= 5 + 2\sqrt{10} + 2 = 7 + 2\sqrt{10}$$

$$\sqrt{(3)^{-2}} = (3^{-2})^{\frac{1}{2}} = 3^{-2 \times \frac{1}{2}} = 3^{-1} = \frac{1}{3}.$$

3. O is a rational number.

4. Let
$$x = 1.8181....(i)$$

100x = 181.8181... ...(ii) [multiplying eqn. (i) by 100]

99x = 180 [subtracting (i) from (ii)]

$$\chi = \frac{180}{99}$$

Hence, 1.8181 ...
$$=\frac{180}{99}=\frac{20}{11}$$

5.
$$\sqrt{45} - 3\sqrt{20} + 4\sqrt{5} = 3\sqrt{5} - 6\sqrt{5} + 4\sqrt{5} = \sqrt{5}$$
.

$$\frac{(0.6)^0 - (0.1)^{-1}}{\left(\frac{3}{8}\right)^{-1} \left(\frac{3}{2}\right)^3 + \left(-\frac{1}{3}\right)^{-1}} = \frac{1}{\frac{8}{3} \times \frac{27}{8} + (-3)} = \frac{1 - 10}{9 - 3} = \frac{-9}{6} = -\frac{3}{2}$$

7.

$$\frac{4}{(216)^{\frac{-2}{3}}} - \frac{1}{(256)^{\frac{-3}{4}}} = 4 \times (216)^{\frac{2}{3}} - (256)^{\frac{3}{4}} = 4 \times (6 \times 6 \times 6)^{\frac{2}{3}} - (4 \times 4 \times 4 \times 4)^{\frac{3}{4}}$$
$$= 4 \times 6^{3 \times \frac{2}{3}} - 4^{4 \times \frac{3}{4}} = 4 \times 6^{2} - 4^{3}$$
$$= 4 \times 36 - 64 = 144 - 64 = 80$$

Short Answer:

Ans: 1.
$$(\sqrt{5} + \sqrt{2})2 + (\sqrt{8} - \sqrt{5}2 = 5 + 2 + 2\sqrt{10} + 8 + 5 - 2\sqrt{40} = 20 + 2\sqrt{10} - 4\sqrt{10} = 20 - 2\sqrt{10}$$

Ans: 2. Let
$$x = 23.43$$

$$100x = 2343.4343...$$
 ...(ii) [Multiplying eqn. (i) by 100]

$$\Rightarrow \chi = \frac{2320}{99}$$

Hence,
$$23.\overline{43} = \frac{2320}{99}$$

Ans: 3. Yes, 'ab' is necessarily an irrational.

For example, let a = 2 (a rational number) and $b = \sqrt{2}$ (an irrational number) If possible let $ab = 2\sqrt{2}$ is a rational number.

Now
$$\frac{ab}{a} = \frac{2\sqrt{2}}{2} = \sqrt{2}$$
 is a rational number.

[: The quotient of two non-zero rational number is a rational]

But this contradicts the fact that V2 is an irrational number.

Thus, our supposition is wrong.

Hence, ab is an irrational number.

Ans: 4. Yes, x + y is necessarily an irrational number.

For example, let x = 3 (a rational number) and $y = \sqrt{5}$ (an irrational number) If possible, let $x + y = 3 + \sqrt{5}$ be a rational number.

Consider $\frac{p}{q} = 3 + \sqrt{5}$, where p, q \in Z and q \neq 0.

Squaring both sides, we have

$$\frac{p^2}{q^2} = 9 + 5 + 6\sqrt{5} \quad \Rightarrow \quad \frac{p^2}{q^2} = 14 + 6\sqrt{5}$$

$$\Rightarrow \frac{p^2}{q^2} - 14 = 6\sqrt{5} \quad \Rightarrow \quad \frac{p^2 - 14q^2}{6q^2} = \sqrt{5}$$

$$\therefore \frac{p}{q} \text{ is a rational} \quad \Rightarrow \frac{p^2 - 14q^2}{6q^2} \text{ is a rational}$$

$$\frac{p}{q}$$
 is a rational

 \Rightarrow V5 is a rational

But this contradicts the fact that V5 is an irrational number.

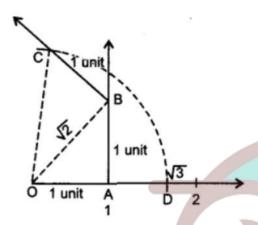
Thus, our supposition is wrong.

Hence, x + y is an irrational number.

Ans: 5.

Here,
$$\sqrt{3} = \sqrt{1+2} = \sqrt{(1)^2 + (\sqrt{2})^2}$$

And, $\sqrt{2} = \sqrt{1+1} = \sqrt{(1)^2 + (1)^2}$



On the number line, take OA = 1 unit. Draw AB = 1 unit perpendicular to OA. Join OB.

Again, on OB, draw BC = 1 unit perpendicular to OB. Join OC.

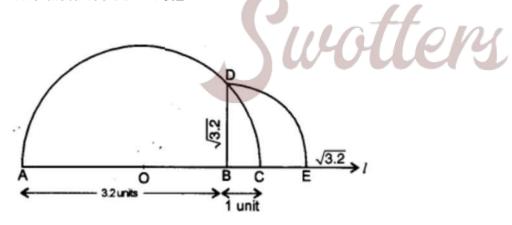
By Pythagoras Theorem, we obtain $OC = \sqrt{3}$. Using

compasses, with Centre O and radius OC, draw an arc, which intersects the number line at point

D. Thus, OD = $\sqrt{3}$ and D corresponds to $\sqrt{3}$.

Ans: 6. First of all draw a line of length 3.2 units such that AB = 3.2 units. Now, from point B, mark distance of 1 unit. Let this point be 'C'. Let 'O' be the mid-point of the distance AC. Now, draw a semicircle with Centre 'O' and radius OC. Let us draw a line perpendicular to AC passing through the point 'B' and intersecting the semicircle at point 'D'.

 \therefore The distance BD = $\sqrt{3.2}$



Now, to represent $\sqrt{3.2}$ on the number line. Let us take the line BC as number line and point 'B' as zero, point 'C' as '1' and so on. Draw an arc with Centre B and radius BD, which intersects the number line at point 'E'.

Then, the point 'E' represents V3.2.

Ans: 7. Let. x = 1.32 = 1.3222.... (i)

Multiplying eq. (i) by 10, we have

10x = 13.222...

Again, multiplying eq. (i) by 100, we have

100x = 132.222... ...(iii)

Subtracting eq. (ii) from (iii), we have

$$100x - 10x = (132.222...) - (13.222...)$$

90x = 119

$$\Rightarrow \chi = \frac{119}{90}$$

Again, y = 0.35 = 0.353535...

Multiply (iv) by 100, we have ...(iv)

100y = 35.353535... (v)

Subtracting (iv) from (u), we have

$$100y - y = (35.353535...) - (0.353535...)$$

99y = 35

$$y = \frac{35}{99}$$

Now,
$$1.3\overline{2} + 0.\overline{35} = x + y = \frac{119}{90} + \frac{35}{99} = \frac{1309 + 350}{990} = \frac{1659}{990} = \frac{553}{330}$$

Long Answer:

Ans: 1.

$$x = \frac{\sqrt{p+q} + \sqrt{p-q}}{\sqrt{p+q} - \sqrt{p-q}} = \frac{\sqrt{p+q} + \sqrt{p-q}}{\sqrt{p+q} - \sqrt{p-q}} \times \frac{\sqrt{p+q} + \sqrt{p-q}}{\sqrt{p+q} + \sqrt{p-q}}$$

$$= \frac{\left(\sqrt{p+q} + \sqrt{p-q}\right)^{2}}{\left(\sqrt{p+q}\right)^{2} - \left(\sqrt{p-q}\right)^{2}} = \frac{p+q+p-q+2 \times \sqrt{p+q} \times \sqrt{p-q}}{(p+q) - (p-q)}$$

$$= \frac{2p+2\sqrt{p^{2}-q^{2}}}{2q} = \frac{p+\sqrt{p^{2}-q^{2}}}{q}$$

$$\Rightarrow qx = p + \sqrt{p^2 - q^2}$$
$$\Rightarrow qx - p = \sqrt{p^2 - q^2}$$

Squaring both sides, we have

$$\Rightarrow q^2x^2 + p^2 - 2pqx = p^2 - q^2$$

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$$\Rightarrow q^{2}x^{2} - 2pqx + q^{2} = 0$$

$$\Rightarrow q (q^{2} - 2px + q) = 0$$

$$\Rightarrow qx^{2} - 2px + q = 0 (: q \neq 0)$$

Ans: 2

Here,
$$a = \frac{1}{3 - \sqrt{11}} \times \frac{3 + \sqrt{11}}{3 + \sqrt{11}} = \frac{3 + \sqrt{11}}{9 - 11} = \frac{3 + \sqrt{11}}{-2}$$

$$b = \frac{1}{a} = 3 - \sqrt{11}$$
Now,
$$a^2 - b^2 = (a + b) (a - b)$$

$$= \left(\frac{3 + \sqrt{11}}{-2} + 3 - \sqrt{11}\right) \left(\frac{3 + \sqrt{11}}{-2} - 3 + \sqrt{11}\right)$$

$$= \left(\frac{-3 - \sqrt{11} + 6 - 2\sqrt{11}}{2}\right) \left(\frac{-3 - \sqrt{11} - 6 + 2\sqrt{11}}{2}\right)$$

$$= \left(\frac{3 - 3\sqrt{11}}{2}\right) \left(\frac{-9 + \sqrt{11}}{2}\right) = \frac{-27 + 3\sqrt{11} + 27\sqrt{11} - 33}{4}$$

$$= \frac{-60 + 30\sqrt{11}}{4} = \frac{-30 + 15\sqrt{11}}{2} = \frac{1}{2}(15\sqrt{11} - 30)$$

Ans: 3

$$\frac{3\sqrt{2}}{\sqrt{6} - \sqrt{3}} - \frac{4\sqrt{3}}{\sqrt{6} - \sqrt{2}} + \frac{2\sqrt{3}}{\sqrt{6} + 2}$$

$$= \frac{3\sqrt{2}}{\sqrt{6} - \sqrt{3}} \times \frac{\sqrt{6} + \sqrt{3}}{\sqrt{6} + \sqrt{3}} - \frac{4\sqrt{3}}{\sqrt{6} - \sqrt{2}} \times \frac{\sqrt{6} + \sqrt{2}}{\sqrt{6} + \sqrt{2}} + \frac{2\sqrt{3}}{\sqrt{6} + 2} \times \frac{\sqrt{6} - 2}{\sqrt{6} - 2}$$

$$= \frac{3\sqrt{12} + 3\sqrt{6}}{(\sqrt{6})^2 - (\sqrt{3})^2} - \frac{4\sqrt{18} + 4\sqrt{6}}{(\sqrt{6})^2 - (\sqrt{2})^2} + \frac{2\sqrt{18} - 4\sqrt{3}}{(\sqrt{6})^2 - (2)^2}$$

$$= \frac{6\sqrt{3} + 3\sqrt{6}}{6 - 3} - \frac{12\sqrt{2} + 4\sqrt{6}}{6 - 2} + \frac{6\sqrt{2} - 4\sqrt{3}}{6 - 4}$$

$$= \frac{6\sqrt{3} + 3\sqrt{6}}{3} - \frac{12\sqrt{2} + 4\sqrt{6}}{4} + \frac{6\sqrt{2} - 4\sqrt{3}}{2}$$

$$= \frac{24\sqrt{3} + 12\sqrt{6} - 36\sqrt{2} - 12\sqrt{6} + 36\sqrt{2} - 24\sqrt{3}}{12} = \frac{0}{12} = 0.$$

Ans: 4.

$$\begin{split} &\frac{1}{1+\sqrt{2}} + \frac{1}{\sqrt{2}+\sqrt{3}} + \frac{1}{\sqrt{3}+\sqrt{4}} + \dots + \frac{1}{\sqrt{8}+3} \\ &= \frac{1}{1+\sqrt{2}} \times \frac{1-\sqrt{2}}{1-\sqrt{2}} + \frac{1}{\sqrt{2}+\sqrt{3}} \times \frac{\sqrt{2}-\sqrt{3}}{\sqrt{2}-\sqrt{3}} + \frac{1}{\sqrt{3}+\sqrt{4}} \times \frac{\sqrt{3}-\sqrt{4}}{\sqrt{3}-\sqrt{4}} + \dots + \frac{1}{\sqrt{8}+3} \times \frac{\sqrt{8}-3}{\sqrt{8}-3} \\ &= \frac{1-\sqrt{2}}{-1} + \frac{\sqrt{2}-\sqrt{3}}{-1} + \frac{\sqrt{3}-\sqrt{4}}{-1} + \dots + \frac{\sqrt{8}-3}{-1} \\ &= -1+\sqrt{2}-\sqrt{2}+\sqrt{3}-\sqrt{3}+\sqrt{4}-\dots - \sqrt{8}+3 \\ &= -1+3=2 \end{split}$$

Ans: 5.

Here,
$$\frac{2\sqrt{5} + \sqrt{3}}{2\sqrt{5} - \sqrt{3}} + \frac{2\sqrt{5} - \sqrt{3}}{2\sqrt{5} + \sqrt{3}} = a + \sqrt{15}b$$

$$\frac{(2\sqrt{5} + \sqrt{3})^2 + (2\sqrt{5} - \sqrt{3})^2}{(2\sqrt{5} - \sqrt{3})(2\sqrt{5} + \sqrt{3})} = a + \sqrt{15}b$$

$$\frac{20 + 3 + 4\sqrt{15} + 20 + 3 - 4\sqrt{15}}{20 - 3} = a + \sqrt{15}b$$

$$\frac{46}{17} = a + \sqrt{15}b$$

Comparing rational and irrational parts, we have

$$a = \frac{46}{17} \text{ and } b = 0$$

Assertion and Reason Answers-

- 1. c) Assertion is correct statement but reason is wrong statement.
- **2.** a) Assertion and reason both are correct statements and reason is correct explanation for assertion.