# **MATHEMATICS**

**Chapter 2: Fractions and Decimals** 



## **Important Questions**

## **Multiple Choice Questions:**

Question 1. What is  $\frac{1}{7}$  of 49 litres?

- (a) 11
- (b) 51
- (c) 71
- (d) 61

Question 2. Find  $\frac{2}{7} \times 3$ .

- (a)  $\frac{5}{7}$
- (b)  $\frac{6}{7}$
- (c)  $\frac{1}{7}$

(d) none of these

Question 3. If 43m = 0.086 then m has the value

- (a) 0.002
- (b) 0.02
- (c) 2
- (d) 0.2

Question 4. Write the place value of 2 in the following decimal numbers: 2.56

- (a) 5
- (b) .06
- (c) 2
- (d) None of these

Question 5. 0.01 × 0.01 = \_\_\_\_\_

- (a) 0.0001
- (b) 0.001
- (c) 1
- (d) 0.1

Question 6. Find 0.2 x 0.3

- (a) 0.6
- (b) 0.06
- (c) 6
- (d) None of these

Question 7. Which of the following is an improper fraction?

- (a)  $\frac{20}{70}$
- (b)  $\frac{30}{40}$
- (c)  $\frac{50}{20}$
- (d)  $\frac{70}{80}$

Question 8. What is  $\frac{1}{2}$  of 10.

- (a) 6
- (b) 4
- (c) 3
- (d) 5

Question 9. Find the area of rectangle whose length is 6.7 cm and breadth is 2 cm.

- (a) 13 cm<sup>2</sup>
- (b) 13.4 cm<sup>2</sup>
- (c) 13.8 cm<sup>2</sup>
- (d) 14 cm<sup>2</sup>

Question 10. Express 5 cm in metre.

- (a) .05
- (b) .5
- (c) .005
- (d) None of these

Question 11. Which amongst the following is the largest?

- (a) -89
- (b) -21

- (c) |-89|
- (d) |-21|

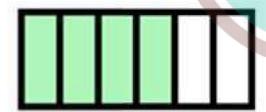
Question 12. The side of an equilateral triangle is 3.5 cm. Find its perimeter.

- (a) 10.5 cm
- (b) 1.05 cm
- (c) 105 cm
- (d) None of these

Question 13. Provide the number in the box  $\cong$  such that  $\frac{3}{5} \times \cong = \frac{24}{75}$ .

- (a)  $\frac{7}{15}$
- (b)  $\frac{8}{15}$
- (c)  $\frac{5}{3}$
- (d) none of these

Question 14. What is the fraction of the shaded area?



- (a)  $\frac{2}{3}$
- (b)  $\frac{1}{3}$
- (c)  $\frac{1}{4}$
- (d) None of these

Question 15. Which of the following is a proper fraction?

- (a)  $\frac{28}{15}$
- (b)  $\frac{21}{23}$
- (c)  $\frac{16}{7}$
- (d)  $\frac{34}{3}$

#### **Very Short Questions:**

- 1. If  $\frac{2}{3}$  of a number is 6, find the number.
- 2. Find the product of  $\frac{6}{7}$  and  $2\frac{2}{3}$ .
- **3.** Solve the following:

$$\frac{2}{3} + \frac{4}{5} \div \frac{2}{5} - 3$$

- **4.** Multiply 2.05 and 1.3.
- **5.** Solve:

(i) 
$$2 - \frac{3}{5}$$
 (ii)  $4 + \frac{7}{8}$  (iii)  $\frac{3}{5} + \frac{2}{7}$ 

**6.** Solve the following:

(a) 
$$3 - \frac{2}{3}$$

(b) 
$$4 + \frac{2}{5}$$

7. Arrange the following in descending order:

(i) 
$$\frac{2}{9}$$
,  $\frac{2}{3}$ ,  $\frac{8}{21}$  (ii)  $\frac{1}{5}$ ,  $\frac{3}{7}$ ,  $\frac{7}{10}$ 

#### **Short Questions:**

1. Arrange the following in ascending order:

(i) 
$$\frac{2}{7}, \frac{3}{5}, \frac{5}{6}$$

(ii) 
$$\frac{1}{5}, \frac{3}{7}, \frac{7}{10}, \frac{1}{6}$$

2. Find the products:

(i) 
$$2.4 \times 100$$

(ii) 
$$0.24 \times 1000$$

- **3.** Arnav spends  $1\frac{3}{4}$  hours in studies,  $2\frac{1}{2}$  hours in playing cricket. How much time did he spend in all?
- **4.** A square paper sheet has  $10\frac{2}{5}$  cm long side. Find its perimeter and area.

**5.** Find the value of 
$$\frac{1}{3\frac{3}{5}} + \frac{1}{4\frac{8}{9}} + \frac{1}{\frac{3}{5}}$$

- 6. The product of two numbers is 2.0016. If one of them is 0.72, find the other number.
- 7. Reemu reads 15th pages of a book. If she reads further 40 pages, she would have read  $\frac{7}{10}$ th page of the book. How many pages are left to be read?
- **8.**  $\frac{1}{8}$  of a number equals  $\frac{2}{5} \div \frac{1}{20}$ . What is the number?

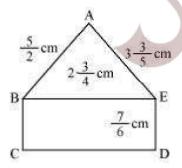
#### **Long Questions:**

Simplify the following:

(i) 
$$\frac{2\frac{1}{2} + \frac{1}{5}}{2\frac{1}{2} \div \frac{1}{5}}$$

(i) 
$$\frac{2\frac{1}{2} + \frac{1}{5}}{2\frac{1}{2} + \frac{1}{5}}$$
 (ii)  $\frac{\frac{1}{4} + \frac{1}{5}}{1 - \frac{3}{8} \times \frac{3}{5}}$ 

- The weight of an object on the Moon is  $\frac{1}{6}$  its weight on the Earth. If an object 2. weight  $5\frac{3}{5}$  kg on the Earth. How much would it weight on the Moon?
- A picture hall has seats for 820 persons. At a recent film show, one usher 3. guessed it was  $\frac{3}{4}$  full, another that it was  $\frac{2}{3}$  full. The ticket office reported 648 sales. Which usher (first or second) made the better guess?
- A rectangular sheet of paper is  $12\frac{1}{2}$  cm long and  $10\frac{2}{3}$  cm wide. 4. Find its perimeter.
- Find the perimeters of (i)  $\triangle ABE$  (ii) the rectangle BCDE in this figure. Whose 5. perimeter is greater?



#### **Assertion and Reason Questions:**

1) Assertion: fraction is a number expressed as a quotient, in which a numerator is divided by a denominator.

**Reason:** 4/11 is a fraction.

- a.) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion
- b.) Both Assertion and Reason are correct and Reason is not the correct explanation for Assertion.
- c.) assertion is true but the reason is false.
- d.) both assertion and reason are false.
- 2) Assertion: 2/7 is an improper fraction.

Reason: in improper fraction numerator is greater than denominator.

- a.) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion
- b.) Both Assertion and Reason are correct and Reason is not the correct explanation for Assertion.
- c.) assertion is true but the reason is false.
- d.) both assertion and reason are false.

#### **ANSWER KEY-**

#### **Multiple Choice questions:**

- **1.** (c) 71
- **2.** (b)  $\frac{6}{7}$
- **3.** (a) 0.002
- **4.** (c) 2
- **5.** (a) 0.0001
- **6.** (b) 0.06
- 7. (c)  $\frac{50}{20}$
- **8.** (d) 5
- **9.** (b) 13.4 cm<sup>2</sup>
- **10.** (a) .05
- **11.** (c) |-89|
- **12.** (a) 10.5 cm
- **13.** (b)  $\frac{8}{15}$

**14.** (a) 
$$\frac{2}{3}$$

**15.** (b) 
$$\frac{21}{23}$$

#### **Very Short Answer:**

1. Let x be the required number.

$$\therefore \frac{2}{3} \text{ of } x = 6 \implies \frac{2}{3} \times x = 6$$

$$\Rightarrow x = 6 \div \frac{2}{3} = 6 \times \frac{3}{2} = 3 \times 3 = 9$$

Hence, the required number is 9.

2.

$$\frac{6}{7} \times 2\frac{2}{3} = \frac{\cancel{6}^2}{7} \times \frac{8}{\cancel{3}} = \frac{2 \times 8}{7 \times 1}$$
$$= \frac{16}{7} = 2\frac{2}{7}$$

3.

$$\frac{2}{3} + \frac{4}{5} \div \frac{2}{5} - 3 = \frac{2}{3} + \frac{\cancel{4}^2}{\cancel{5}} \times \frac{\cancel{5}}{\cancel{2}} - 3$$
$$= \frac{2}{3} + 2 - 3 = \frac{2}{3} - 1 = \frac{2 - 3}{3} = -\frac{1}{3}$$

4.

$$2.05 \times 1.3 = \frac{205}{100} \times \frac{13}{10} = \frac{2665}{1000} = 2.665$$

5.

(i) 
$$2 - \frac{3}{5} = \frac{2 \times 5}{5} - \frac{3}{5} = \frac{10 - 3}{5} = \frac{7}{5}$$

(ii) 
$$4 + \frac{7}{8} = \frac{4 \times 8}{8} + \frac{7}{8} = \frac{(4 \times 8) + 7}{8} = \frac{39}{8} = 4\frac{7}{8}$$

(iii) 
$$\frac{3}{5} + \frac{2}{7} = \frac{3 \times 7}{5 \times 7} + \frac{2 \times 5}{7 \times 5} = \frac{21 + 10}{35} = \frac{31}{35}$$

6.

(a) 
$$3 - \frac{2}{3} = \frac{3}{1} - \frac{2}{3} = \frac{3 \times 3 - 2 \times 1}{3}$$
  
=  $\frac{9 - 2}{3} = \frac{7}{3} = 2\frac{1}{3}$ 

(b) 
$$4 + \frac{2}{5} = \frac{4}{1} + \frac{2}{5} = \frac{4 \times 5 + 2 \times 1}{5}$$
  
=  $\frac{20 + 2}{5} = \frac{22}{5} = 4\frac{2}{5}$ 

**7**.

(i) 
$$\frac{2}{9}$$
,  $\frac{2}{3}$ ,  $\frac{8}{21}$ 

Changing them to like fractions, we obtain

$$\frac{2}{9} = \frac{2 \times 7}{9 \times 7} = \frac{14}{63}$$

$$\frac{2}{3} = \frac{2 \times 21}{3 \times 21} = \frac{42}{63}$$

$$\frac{8}{21} = \frac{8 \times 3}{21 \times 3} = \frac{24}{63}$$

Since 42>24>14,

$$\therefore \frac{2}{3} > \frac{8}{21} > \frac{2}{9}$$

(ii) 
$$\frac{1}{5}$$
,  $\frac{3}{7}$ ,  $\frac{7}{10}$ 

Changing them to like fractions, we obtain

$$\frac{1}{5} = \frac{1 \times 14}{5 \times 14} = \frac{14}{70}$$
$$\frac{3}{7} = \frac{3 \times 10}{7 \times 10} = \frac{30}{70}$$
$$\frac{7}{10} = \frac{7 \times 7}{10 \times 7} = \frac{49}{70}$$

As 49 > 30>14,

$$\therefore \frac{7}{10} > \frac{3}{7} > \frac{1}{5}$$

#### **Short Answer:**

1.

(i) We have 
$$\frac{2}{7}, \frac{3}{5}$$
 and  $\frac{5}{6}$ 

LCM of 7, 5 and 6 = 210

Since, the denominators are same.

Hence, the required order is

$$\frac{5}{6} > \frac{3}{5} > \frac{2}{7}$$

(ii) We have 
$$\frac{1}{5}, \frac{3}{7}, \frac{7}{10}$$
 and  $\frac{1}{6}$ 

LCM of 5, 7, 10 and 6 = 210

$$\frac{1}{5} \times \frac{42}{42} = \frac{42}{210}$$

$$\frac{3}{7} \times \frac{30}{30} = \frac{90}{210}$$

$$\frac{7}{10} \times \frac{21}{21} = \frac{147}{210}$$

$$\frac{1}{5} \times \frac{42}{42} = \frac{42}{210}$$

$$\frac{2}{3} \times \frac{5}{7}, \frac{7}{10}, \frac{6}{6}$$

$$\frac{3}{5} \times \frac{5}{7}, \frac{5}{5}, \frac{3}{5}$$

$$\frac{7}{1}, \frac{7}{1}, \frac{1}{1}, \frac{1}{1}$$

$$1, \frac{1}{1}, \frac{1}{1}, \frac{1}{1}$$

$$1 \times \frac{1}{1} \times \frac{1}{1} \times \frac{1}{1}$$

$$1 \times \frac{1}{1}$$

$$\frac{1}{6} \times \frac{35}{35} = \frac{35}{210}$$

Since, the denominator are same.

$$\therefore 147 > 90 > 42 > 35$$

Hence, the required order is  $\frac{7}{10} > \frac{3}{7} > \frac{1}{5} > \frac{1}{6}$ .

2.

(i) 
$$2.4 \times 100 = \frac{24}{10} \times 100 = 24 \times 10 = 240$$

(ii) 
$$0.24 \times 1000 = \frac{24}{100} \times 1000 = 24 \times 10 = 240$$

(iii) 
$$0.024 \times 10000 = \frac{24}{1000} \times 10000$$
  
=  $24 \times 10 = 240$ 

3. Time spent by Arnav in studies =  $1\frac{3}{4}$  hours

Time spent by Arnav in playing cricket =  $2\frac{1}{2}$  hours

Total time spent by Arnav =  $1\frac{3}{4}$  hours +  $2\frac{1}{2}$  hours

$$= \left(\frac{7}{4} + \frac{5}{2}\right) \text{ hours} = \left(\frac{7 \times 1 + 5 \times 2}{4}\right) \text{hours}$$

$$=$$
  $\left(\frac{7+10}{4}\right)$  hours  $=\frac{17}{4}$  hours or  $4\frac{1}{4}$  hours

4.

Length of the side of the square sheet

$$= 10\frac{2}{5} \text{ cm} = \frac{52}{5} \text{ cm}$$
Perimeter =  $4 \times \text{side} = 4 \times \frac{52}{5}$ 

$$= \frac{208}{5} \text{ cm} = 41\frac{3}{5} \text{ cm}$$

$$= \frac{208}{5} \text{ cm} = 41\frac{3}{5} \text{ cm}$$

$$= \frac{5}{3}$$

Area = Side × Side = 
$$10\frac{2}{5} \times 10\frac{2}{5}$$
  
=  $\frac{52}{5} \times \frac{52}{5} = \frac{2704}{25}$ 
=  $108\frac{4}{25}$  cm<sup>2</sup>

$$= \frac{25}{204}$$
=  $204$ 

5.

$$\frac{1}{3\frac{3}{5}} + \frac{1}{4\frac{8}{9}} + \frac{1}{\frac{3}{5}} = \frac{1}{\left(\frac{18}{5}\right)} + \frac{1}{\left(\frac{44}{9}\right)} + \frac{1}{\left(\frac{3}{5}\right)}$$

$$= \frac{5}{18} + \frac{9}{44} + \frac{5}{3}$$

$$= \frac{2 \mid 18, 44, 3}{2 \mid 9, 22, 3}$$

$$= \frac{3 \mid 9, 11, 3}{3 \mid 3, 11, 1}$$

$$= \frac{11}{11, 11, 1}$$

$$= \frac{11}{11, 11, 1}$$

Hence, the required value is  $2\frac{59}{396}$ .

**6.** Product of two numbers = 2.0016

One number = 0.72

Other number =  $2.0016 \div 0.72$ 

$$= \frac{2.0016}{0.72} = \frac{20016}{10000} \times \frac{100}{72}$$
$$= \frac{139}{50} = \frac{139 \times 2}{50 \times 2} = \frac{278}{100} = 2.78$$

Hence, the required number = 2.78.

7. Let the total number of pages be x.

Number of pages read by Reemu =  $\frac{1}{5x}$ 

If she reads 40 more pages,

Total number of pages read by her =  $\frac{1}{5}x + 40$ 

$$\frac{7}{10}x = \frac{1}{5}x + 40 \implies \frac{7}{10}x - \frac{1}{5}x = 40$$

$$\Rightarrow \frac{7x - 2x}{10} = 40 \Rightarrow \frac{5x}{10} = 40$$

$$\Rightarrow \qquad x = 40 \div \frac{5}{10} = 40 \times \frac{\cancel{10}^2}{\cancel{5}} = 80$$

Hence, the required number of pages = 80.

**8.** Let the number be x.

$$\therefore \frac{1}{8} \text{ of } x = \frac{2}{5} \div \frac{1}{20}$$

$$\Rightarrow \frac{1}{8} \times x = \frac{2}{5} \times \frac{20^4}{1}$$

$$\Rightarrow \frac{1}{8} x = 2 \times 4 \Rightarrow \frac{1}{8} x = 8$$

$$\Rightarrow x = 8 \times 8 = 64$$

Hence, the required number = 64.

#### Long Answer:

1.

(i) 
$$\frac{2\frac{1}{2} + \frac{1}{5}}{2\frac{1}{2} + \frac{1}{5}} = \frac{\frac{5}{2} + \frac{1}{5}}{\frac{5}{2} + \frac{1}{5}} = \frac{\frac{5 \times 5 + 1 \times 2}{10}}{\frac{5}{2} \times \frac{5}{1}}$$

$$= \frac{\frac{25 + 2}{10}}{\frac{25}{2}} = \frac{27}{\cancel{10}_{5}} \times \frac{\cancel{2}}{25} = \frac{27}{125}$$
(ii) 
$$\frac{\frac{1}{4} + \frac{1}{5}}{1 - \frac{3}{8} \times \frac{3}{5}} = \frac{\frac{5 + 4}{20}}{1 - \frac{9}{40}} = \frac{\frac{9}{20}}{\frac{40 - 9}{40}} = \frac{\frac{9}{20}}{\frac{31}{40}}$$

$$= \frac{9}{\cancel{20}} \times \frac{\cancel{40}^{2}}{31} = \frac{9 \times 2}{31} = \frac{18}{31}$$

2. Weight of the object on the Earth

$$=5\frac{3}{5} \text{ kg} = \frac{28}{5} \text{ kg}$$

 $\therefore$  Weight of the object on the Earth

$$=\frac{1}{62} \times \frac{28^{14}}{5} \text{ kg} = \frac{14}{15} \text{ kg}$$

Hence, the required weight  $=\frac{14}{15}$  kg.

3. Total number of seats = 820

Number of ticket sold = 648

For first usher = 
$$\frac{3}{4} \times 648 = 3 \times 162 = 486$$

For second usher = 
$$\frac{2}{3} \times 648 = 2 \times 216 = 432$$

Since 432 < 486

Hence, the first usher guessed better.

4. Length =  $12\frac{1}{2}$  cm =  $\frac{25}{2}$  cm

Breadth = 
$$10\frac{2}{3}$$
 cm =  $\frac{32}{2}$  cm

Perimeter = 2 × (Length + Breadth)

$$= 2 \times \left[ \frac{25}{2} + \frac{32}{3} \right] = 2 \times \left[ \frac{(25 \times 3) + (32 \times 2)}{6} \right] = 2 \times \left[ \frac{75 + 64}{6} \right]$$

$$=2\times\frac{139}{6}=\frac{139}{3}=46\frac{1}{3}$$
cm

5. (i) Perimeter of  $\triangle ABE = AB + BE + EA$ 

$$= \left(\frac{5}{2} + 2\frac{3}{4} + 3\frac{3}{5}\right) = \left(\frac{5}{2} + \frac{11}{4} + \frac{18}{5}\right)$$

$$= \left(\frac{5 \times 10}{2 \times 10} + \frac{11 \times 5}{4 \times 5} + \frac{18 \times 4}{5 \times 4}\right)$$

$$=\frac{50+55+72}{20}=\frac{177}{20}=8\frac{17}{20}$$
cm

(ii) Perimeter of rectangle = 2 (Length + Breadth)

Perimeter of rectangle = 
$$2\left[\frac{11}{4} + \frac{7}{6}\right]$$
  
=  $2\left[\frac{11 \times 3}{4 \times 3} + \frac{7 \times 2}{6 \times 2}\right] = 2\left[\frac{33 + 14}{12}\right]$ 

$$=2\times\frac{47}{12}=\frac{47}{6}=7\frac{5}{6}$$
cm

Perimeter of  $\Delta ABE = \frac{177}{20} \text{ cm}$ 

Changing them to like fractions, we obtain

$$\frac{177}{20} = \frac{177 \times 3}{20 \times 3} = \frac{531}{60}$$

$$\frac{47}{6} = \frac{47 \times 10}{6 \times 10} = \frac{470}{60}$$

As 531 > 470,

$$\Rightarrow \frac{177}{20} > \frac{47}{6}$$

Perimeter (ΔABE) > Perimeter (BCDE)

#### **Assertion and Reason Questions:**

- 1) a) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion.
- 2) d.) both assertion and reason are false.

